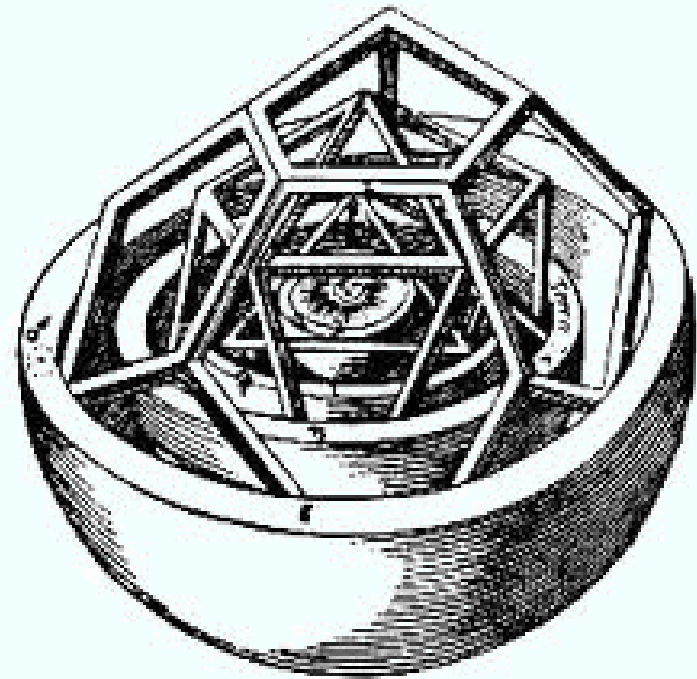
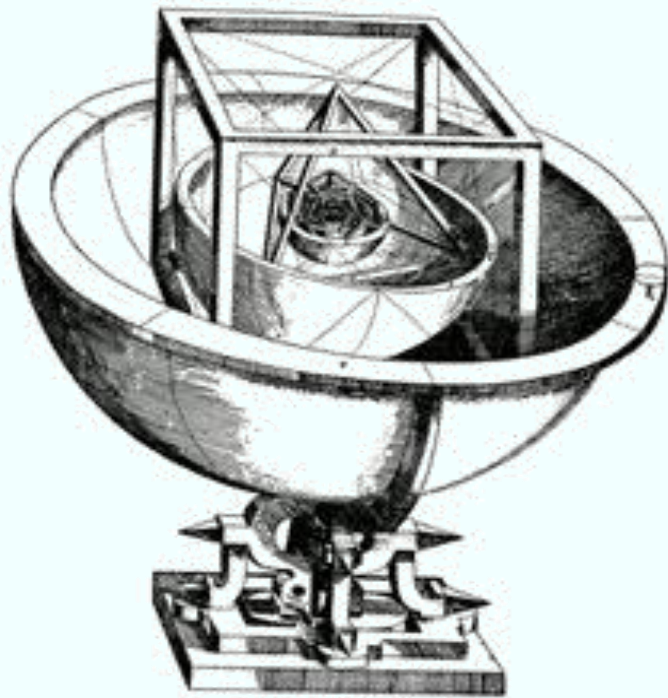
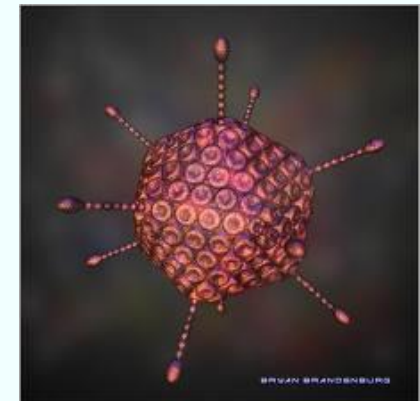
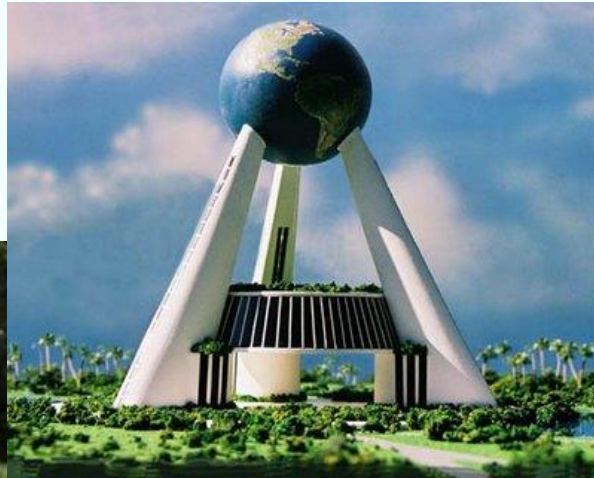


Johannes Kepler's Model of the Solar System

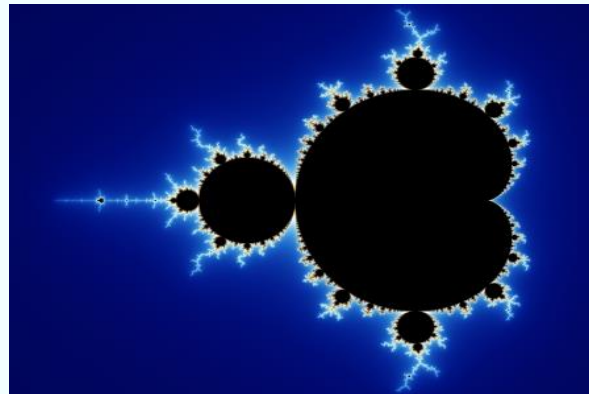
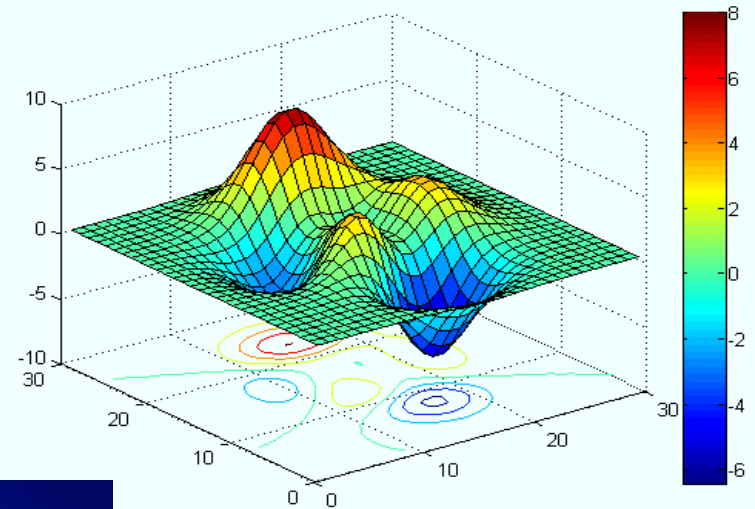
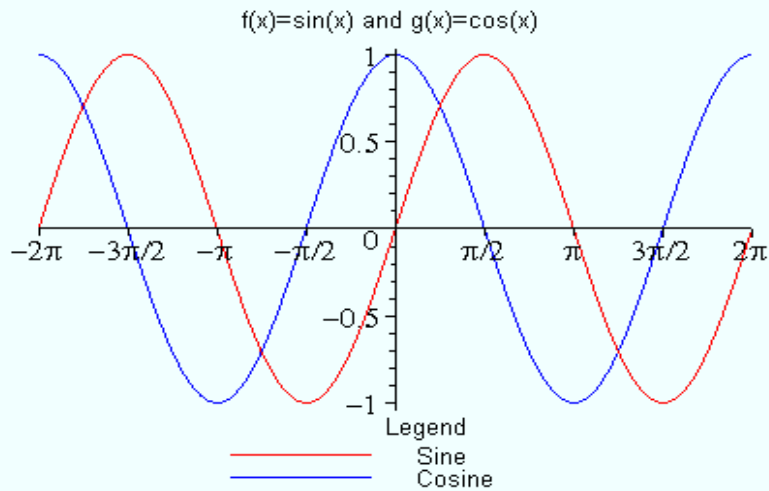
(*Mysterium Cosmographicum*, 1596)



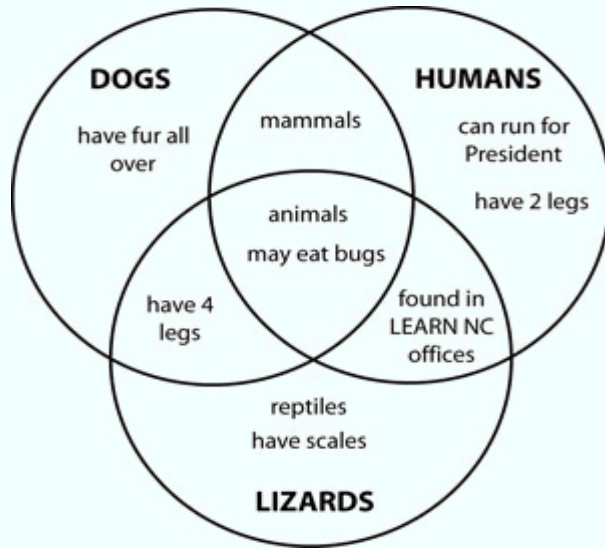
Regular Polyhedral Structures in the Real World



Math Models as Graphical Representations



Math Models as Symbolic/Tabular Representations



$$\int_a^b f(x) dx = F(b) - F(a).$$

Table 2. COF and values for the mixture design experiments for the mobile phase of the HPLC carbohydrate analysis

| Experiments | Mobile Phases ^a | PIRs values | COF values <i>R</i> _d = 1.2 |
|-------------|----------------------------|-------------|---|
| 1 | 50:10:40 | 1.230 | 0.016 |
| 2 | 70:10:20 | 1.066 | -0.085 |
| 3 | 60:14:26 | 0.788 | -0.422 |
| 4 | 60:10:30 | 1.206 | 0.005 |
| 5 | 55:12:33 | 1.071 | -0.114 |
| 6 | 65:12:23 | 0.965 | -0.218 |
| 7 | 60:11.3:28.7 | 1.044 | -0.140 |
| 8 | 55:10.4:34.6 | 1.156 | -0.037 |
| 9 | 65:11.7:23.3 | 1.037 | -0.245 |
| 10 | 50:10:40 | 1.212 | 0.009 |
| 11 | 70:10:20 | 1.106 | -0.082 |
| 12 | 60:14:26 | 0.787 | -0.426 |
| 13 | 60:10:30 | 1.205 | 0.0042 |
| 14 | 55:12:33 | 1.073 | -0.112 |
| 15 | 65:12:23 | 0.971 | -0.212 |
| 16 | 60:11.3:28.7 | 1.045 | -0.138 |
| 17 | 60:11.3:28.7 | 1.061 | -0.123 |
| 18 | 60:11.3:28.7 | 1.058 | -0.126 |
| 19 | 60:11.3:28.7 | 1.061 | -0.123 |
| 20 | 60:11.3:28.7 | 1.045 | -0.138 |

^a acetonitrile, water and ethyl acetate, respectively.



Math Models of Nature and Architectures

Catenaries and the *hyperbolic cosine* function



$$y = a \cosh\left(\frac{x}{a}\right) = \frac{a}{2} \left(e^{x/a} + e^{-x/a}\right)$$



The Top Ten Laws of Our World

(Robert Crease: *A Brief Guide to the Great Equations*, 2009)

1. The Pythagorean Theorem $a^2 + b^2 = c^2$
2. Newton's 2nd Law of Motion $F = ma$
3. Newton's Law of Universal Gravitation $F = G \frac{mM}{r^2}$
4. Euler's Formula $e^{ix} = \cos x + i \sin x$
5. The 2nd Law of Thermodynamics $\Delta S = \int \frac{\delta q}{T}$.

The Top Ten Laws of Our World

(Robert Crease: *A Brief Guide to the Great Equations*, 2009)

$$\nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t} - \vec{M}$$

$$\nabla \times \vec{H} = -\frac{\partial \vec{D}}{\partial t} + \vec{J}$$

$$\nabla \cdot \vec{D} = \rho$$

$$\nabla \cdot \vec{B} = 0$$

6. Maxwell's Equations

7. Einstein's Mass-Energy Equivalence $E = mc^2$

8. Einstein's Field Equations $R_{\mu\nu} - \frac{1}{2}Rg_{\mu\nu} + \Lambda g_{\mu\nu} = 8\pi \frac{G}{c^4}T_{\mu\nu}$

9. Schrödinger's Equation $i\hbar \frac{\partial}{\partial t}\Psi(x, t) = \hat{H}\Psi(x, t)$

10. The Heisenberg Uncertainty Principle $\Delta\chi\Delta\rho \geq \frac{\hbar}{2}$

Structures of Basic Types of Models in School Arithmetic and Algebra

- Additive : $A + B = C$, $C - B = A$, $C - A = B$; $A \pm x = C$
- Multiplicative: $AB = C$, $C/B = A$, $C/A = B$; $Ax = C$
- Proportional: $A/B = C/D$, $B/A = D/C$, $A/C = B/D$, $C/A = D/B$
- Percent and percent change:
 $A \div B = c\%$, $A \div c\% = B$, $B * c\% = A$;
 $C = P \pm P * r\% = P(1 \pm r\%)$

Structures of Basic Types of Models in School Arithmetic and Algebra

- Recursive: $a_n - a_{n-1} = c$; $a_n / a_{n-1} = c$
- Linear: $Ax + B = C$; $y = mx + b$; $Ax + By + C = 0$
- Nonlinear (quadratic, power, radical, polynomial, rational, exponential, logarithmic, trigonometric, etc.)
- Absolute value and piecewise models
- Combinations of the above
- Inequality versions of the above